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Version of attached file:

Published Version

Peer-review status of attached file:

Peer-reviewed

Citation for published item:

Zhao, H. and Macciò, A. and Li, B. and Hoekstra, H. and Feix, M. (2010) 'Structure formation by fifth force : power spectrum from N-body simulations.', *Astrophysical journal letters*, 712 (2). L179-L183.

Further information on publisher's website:

<http://dx.doi.org/10.1088/2041-8205/712/2/L179>

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STRUCTURE FORMATION BY FIFTH FORCE: POWER SPECTRUM FROM N -BODY SIMULATIONS

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Received 2009 October 15; accepted 2010 February 8; published 2010 March 17

ABSTRACT

We lay out the framework to numerically study nonlinear structure formation in the context of scalar-field-coupled cold dark matter models (φ CDM models) where the scalar field φ serves as dynamical dark energy. Adopting parameters for the scalar field that leave negligible effects on the cosmic microwave background (CMB) spectrum, we generate the initial conditions for our N -body simulations. The simulations follow the spatial distributions of dark matter and the scalar field, solving their equations of motion using a multilevel adaptive grid technique. We show that the spatial configuration of the scalar field depends sensitively on the local density field. The φ CDM model differs from standard Λ CDM at small scales with observable modifications of, e.g., the mass function of halos as well as the matter power spectrum. Nevertheless, the predictions of both models for the Hubble expansion and the CMB spectrum are virtually indistinguishable. Hence, galaxy cluster counts and weak lensing observations, which probe structure formation at small scales, are needed to falsify this class of models.

Key words: cosmology: theory – methods: numerical

Online-only material: color figures

1. INTRODUCTION

The origin and nature of dark energy (Copeland et al. 2006) is one of the most difficult challenges facing physicists and cosmologists at the present time. Among all the proposed models to tackle this problem, the introduction of a scalar field is perhaps the most popular. The scalar field, denoted by φ , should have no coupling to normal matter to be consistent with stringent constraints from experiments (Will 2006, and references therein), but could couple to the dark matter, therefore producing a fifth force between dark matter particles. This idea has gained a lot of interest in recent years because dark matter physics are unknown, and such a coupling could alleviate the coincidence problem of dark energy (e.g., Amendola 2000; Chiba 2001; Chimento et al. 2003). Furthermore, it is commonly predicted by low-energy effective theories derived from a more fundamental theory. A specific and interesting possibility is the chameleon mechanism (Khouri & Weltman 2004; Mota & Shaw 2006), by virtue of which the scalar field acquires a large mass in high-density regions and thus the fifth force becomes undetectable on short ranges, thus also evading constraints from the large-scale cosmic microwave background (CMB). Indeed, at the linear perturbation level, there have been a lot of studies about the coupled scalar field and $f(R)$ gravity models (e.g., Li & Barrow 2007; Hu & Sawicki 2007).

Nevertheless, little is known about these models on nonlinear scales. It is well known that the matter distribution at late times, i.e., $z \lesssim 2$ for cluster scales, evolves in a nonlinear way, making the behavior of the scalar field more complex and the linear analysis insufficient to produce accurate results that can be confronted with observations. For the latter purpose, the best way forward is to perform full N -body simulations (Bertschinger 1998) to evolve the individual particles step by step.

N -body simulations including scalar fields and related models have been performed before (Linder & Jenkins 2003; Mainini et al. 2003; Macciò et al. 2004; Springel & Farrar 2007; Kesden

& Kamionkowski 2006a, 2006b; Farrar & Rosen 2007; Baldi et al. 2010; Oyaizu 2008; Keselman et al. 2010; Li & Zhao 2009). For example, in the work of Macciò et al. (2004), the simulations included several effects due to the coupling between dark energy and dark matter (e.g., modified gravitational constant, an extra dragging term in Newton’s equations and time variable dark matter particle masses), but did not consider a spatial variation of the dark energy scalar field. The more complete simulation of the scalar field by Li & Zhao (2009) shows that this approximation is only good for a limited choice of parameters and the scalar field potential. Here we extend the work of Li & Zhao (2009).

This Letter is organized as follows: in Section 2, we shall briefly review the general equations of motion for the coupled scalar field model introduced in Li & Zhao (2009), and present our specific choices of the coupling function and the scalar field potential. In Section 3, we describe the formulae and the algorithm of the N -body simulation, analyze the results of our coupled scalar field N -body simulations, compare it with that of the standard Λ CDM model, and explain the physical origin of the new features. Finally, we conclude and discuss observational implications in Section 4.

2. THE COUPLED SCALAR FIELD MODEL

2.1. The Model

All properties of our coupled scalar field model can be derived from minimizing the action associated with the following Lagrangian density (the index a runs from 0 to 3):

$$\mathcal{L} = \left[\frac{R}{2} - \frac{1}{2} \nabla^a \varphi \nabla_a \varphi + V_{\text{eff}}(\varphi) \right], \quad (1)$$

which includes the Ricci scalar R , and a dimensionless scalar field φ with a kinetic and an effective potential term. The latter is given by

$$V_{\text{eff}}(\varphi) \equiv V(\varphi) - \kappa(\varphi) \mathcal{L}_{\text{CDM}}, \quad (2)$$

where the potential and the coupling function $\kappa(\varphi)$ are controlled by two dimensionless parameters, μ and γ , respectively. More rigorously, the potential $V(\varphi)$ is

$$V(\varphi) = \Lambda_0 [1 - \exp(-\varphi)]^{-\mu} \quad (3)$$

and the coupling function $\kappa(\varphi) \equiv 8\pi G \exp(\gamma\varphi)$, as given in Li & Zhao (2009), where Λ_0 is a constant on the order of the cosmological constant, and G is Newton's constant of gravitation. Considering the nonrelativistic, weak field limit of Equation (2),

$$V_{\text{eff}}(\varphi) \approx \Lambda_0 \varphi^{-\mu} + 8\pi G(1 + \gamma\varphi)\rho_{\text{CDM}}, \quad (4)$$

the meaning of this particular parameterization can be understood as follows: as the scalar field φ tends to minimize the effective potential, the potential term $\Lambda_0 \varphi^{-\mu}$ and the coupling $(1 + \gamma\varphi)$ to the cold dark matter (CDM) density ($\rho_{\text{CDM}} \sim -\mathcal{L}_{\text{CDM}}$ in the nonrelativistic, weak-field limit) lead to competing effects, favoring smaller and larger values of φ , respectively.⁶ The balance of these two effects, minimizing the effective potential V_{eff} , is controlled by the two dimensionless parameters μ and γ : μ is very small and controls the time when the effect of the scalar field (mainly exerting the finite-ranged fifth force on dark matter particles on galaxy cluster scales) becomes important for cosmology while γ determines how large it will ultimately be (Li & Zhao 2009). More specifically, the scalar field equation of motion is

$$\square\varphi + \frac{\partial V(\varphi)}{\partial \varphi} + \rho_{\text{CDM}} 8\pi G \gamma \exp(\gamma\varphi) = 0. \quad (5)$$

Einstein's equations can be expressed as

$$\frac{1}{8\pi G} G_{ab} = \exp(\gamma\varphi) \rho_{\text{CDM}} u_a u_b + T_{ab}^\varphi, \quad (6)$$

where G_{ab} is the Einstein tensor, and the right-hand side is the energy-momentum tensor of the scalar field and CDM with a four-velocity u^a ; the scalar field is given by

$$8\pi G T_{ab}^\varphi = \nabla_a \varphi \nabla_b \varphi - g_{ab} \left[\frac{1}{2} \nabla_c \varphi \nabla^c \varphi - V(\varphi) \right]. \quad (7)$$

Note that the energy-momentum tensors for the scalar field φ and the dark matter are not individually conserved due to their coupling, whereas their sum is.

Equations (5) and (6) summarize all the physics that will be used in our analysis. An immediate application is the prediction of a uniform Hubble expansion. The model's expansion is completely indistinguishable from Λ CDM for values of $\gamma \sim \mathcal{O}(1)$ and $\mu \ll 1$; the actual difference is on the order of $\mathcal{O}(\mu)$. Basically, this is due to the large enough scalar's mass, forcing the field near the potential minimum, which itself is almost time independent for $\mu \ll 1$. A quantitative explanation is given in Li & Zhao (2009). We now proceed to break the degeneracy via nonlinear clustering.

2.2. The Nonrelativistic Equations

The first step toward a numerical simulation is to simplify the relevant equations of motion in the nonrelativistic and quasi-static limit (in the sense that the time derivatives can be safely neglected compared with the spatial derivatives).

⁶ The dark matter Lagrangian \mathcal{L}_{CDM} specifies the geodesic flow for many pointlike particles of four-velocity u_a and density ρ_{CDM} .

Li & Zhao (2009) showed that the scalar equation of motion, Equation (5), and the Poisson equation can be simplified as

$$\frac{\partial_{\mathbf{x}}^2 \varphi}{a^2} \approx 8\pi G \gamma [\rho_{\text{CDM}} - \bar{\rho}_{\text{CDM}}] - \mu \Lambda_0 [\varphi^{-\mu-1} - \bar{\varphi}^{-\mu-1}] \quad (8)$$

$$\frac{\partial_{\mathbf{x}}^2 \Phi}{a^3} \approx 4\pi G [\rho_{\text{CDM}} - \bar{\rho}_{\text{CDM}}] - \Lambda_0 [\varphi^{-\mu} - \bar{\varphi}^{-\mu}]. \quad (9)$$

Note that the above two equations have similar source terms, partly from matter and partly from the scalar field.⁷

Finally, the equations of motion of the dark matter particles are also modified as

$$\frac{d\mathbf{x}}{dt} = \frac{\mathbf{p}}{a^2}, \quad (10)$$

$$\frac{d\mathbf{p}}{dt} = -\frac{1}{a} \bar{\nabla}_{\mathbf{x}} \Phi - \gamma \bar{\nabla}_{\mathbf{x}} \varphi, \quad (11)$$

where the canonical momentum conjugate to the comoving coordinates \mathbf{x} is $\mathbf{p} = a^2 \dot{\mathbf{x}}$. Note that the two terms on the right-hand side of Equation (11) correspond to gravity and fifth force, respectively (Li & Zhao 2009). The scalar field φ is on the order of magnitude of μ , comparable to the dimensionless potential Φ . Equations (8)–(11) are used in the code to evaluate the forces on the dark matter particles and to evolve their positions and momenta in time.

The validity and limitation of the approximation present in the above equations, in particular neglecting the time derivatives, have been extensively discussed in Li & Zhao (2009). We emphasize that these approximations do not hold in the linear regime where the scalar field's time dependence is essential for structure growth. However, such terms have indeed been shown to be negligible on scales much smaller than the horizon scale (Li & Zhao 2009; Oyaizu 2008). To make our predictions more quantitative and rigorous compared to previous analyses (Macciò et al. 2004; Kesden & Kamionkowski 2006a, 2006b; Farrar & Rosen 2007), we now analyze the first N -body simulations in the above framework. Considering the linear regime, Li & Zhao (2009) have already been able to constrain the parameters μ and γ to a fairly narrow range. Here we set γ on the order of unity to force a significant ratio of the fifth force to gravity ($\sim 2\gamma$), and explore the range $10^{-7} \leq \mu \leq 10^{-5}$, covering 3 orders of magnitude. Restricting ourselves to the above should suffice as the model is either essentially indistinguishable from Λ CDM or deviates too much from it (already at the linear level) beyond this parameter space, thus being of no further interest (Li & Zhao 2009).

3. NONLINEAR STRUCTURE FORMATION

In this section, we present some results of the first N -body runs and describe the qualitative behavior of the coupled scalar field model.

3.1. The N -body Code

We adapt the multi-level adaptive particle mesh (MLAPM) code (Knebe et al. 2001) to include the scalar field, and its coupling to the dark matter N -body particles. One benefit of the

⁷ The notation $\partial_{\mathbf{x}}^2 = -\bar{\nabla}_{\mathbf{x}}^2 = \partial_x^2 + \partial_y^2 + \partial_z^2$ is defined with respect to the comoving coordinate \mathbf{x} such that $\bar{\nabla}_{\mathbf{x}} = a \bar{\nabla}_{\mathbf{r}}$, where a is the usual scale factor of the universe. In the following, $\bar{\varphi}$ and $\bar{\rho}_{\text{CDM}}$ denote the background values of φ and ρ_{CDM} , respectively. Although we have used the approximation $\rho_{\text{CDM}} \exp(\gamma\varphi) \sim \rho_{\text{CDM}}$ for a simpler presentation, we keep the factor $\exp(\gamma\varphi)$ as well as the potential given by Equation (3) in the actual simulation.

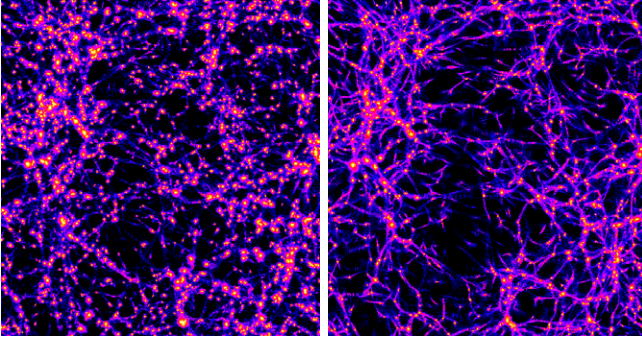


Figure 1. Overdensity fields at $z = 0$ for the ϕ CDM model with $\gamma = 1$, $\mu = 10^{-5}$ (left) and the Λ CDM model (right). The former has developed more small-scale structure within the void.

(A color version of this figure is available in the online journal.)

adaptive scheme is that the majority of computing resources is dedicated to few high-density regions to ensure higher resolution, which is desirable since we expect the behavior of the scalar field to be more complex there.

The main modifications to the MLAPM code for our model are as follows:

1. We have added a parallel solver for the scalar field based on Equation (8). The solver uses a similar nonlinear Gauss–Seidel method (Briggs et al. 2000; Press et al. 1992) and the same criterion for convergence as the Poisson solver.
2. The resulting value for ϕ of the first step is used to calculate the local mass density of the scalar field and thus the source term for Poisson’s equation, which is solved using a fast Fourier transform to obtain the local gravitational potential Φ (cf. Equation (9)).
3. The fifth force is obtained by differentiating ϕ , and the gravitational force is calculated by differentiating Φ , as in Equations (10) and (11).
4. The momenta and positions of particles are then updated, taking into account both gravity and the fifth force, just as in normal N -body codes.

More technical details on the code, as well as how Equations (8)–(11) are incorporated into MLAPM using its own internal units, have been given in Li & Zhao (2009) and will not be presented here.

3.2. Numerical Results from the N -body Runs

We have performed six runs of the modified code with parameters $\gamma = 0.5, 1$ and $\mu = 10^{-5}, 10^{-6}, 10^{-7}$, respectively. For all these runs, there are 128^3 dark matter particles, and the simulation box size is chosen as $B = 64 h^{-1}$ Mpc, with h being the usual dimensionless Hubble parameter and 128 domain grid cells in each direction. We assume a Λ CDM background cosmology which is a very good approximation for $\mu \ll 1$ (Li & Zhao 2009); in addition, we adopt present values for the fractional energy densities of dark matter and dark energy, $\Omega_{\text{CDM}} = 0.28$ and $\Omega_{\Lambda} = 0.72$, and the normalization of the power spectrum is chosen as $\sigma_8 = 0.88$. Note that the simulation does only take dark matter into account, baryons will be added in a forthcoming work to study the bias effect caused by the dark matter coupling. Given these parameters, the mass and spatial resolution of the simulation are $9.71 \times 10^9 M_{\odot}$ and $\sim 23.44 h^{-1}$ kpc (for the most refined regions), respectively. This spatial resolution in high-density regions is necessary and sufficient to precisely probe the scalar field in regions where the fifth force is considerably short-ranged.

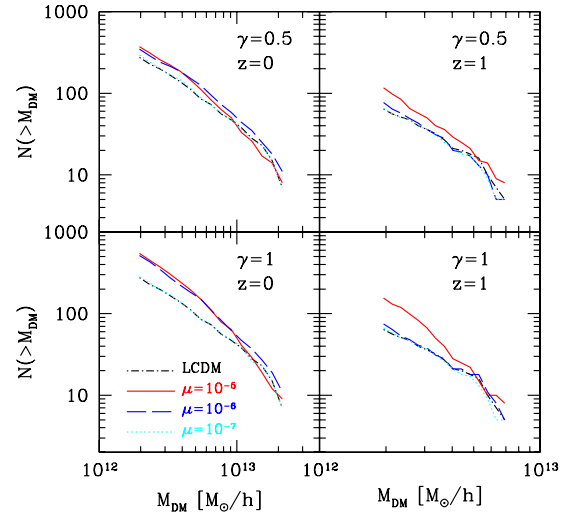


Figure 2. Mass functions for $\gamma = 0.5$ (upper panels) and $\gamma = 1$ (lower panels) for different values of μ at $z = 0$ and $z = 1$. The Λ CDM mass function is also plotted as a (black) dot-dashed curve for comparison.

(A color version of this figure is available in the online journal.)

All simulations started at redshift $z = 49$. In principle, modified initial conditions, i.e., the initial displacements and velocities of particles which are obtained from a given linear matter power spectrum, need to be generated for the coupled scalar field model because the Zel’dovich approximation (Efstathiou et al. 1985) is also affected by the scalar field coupling. In practice, however, we find that the effect on the linear matter power spectrum at this high redshift is negligible ($\lesssim \mathcal{O}(10^{-4})$) for our choice of the parameters γ and μ . Thus we simply use the Λ CDM initial displacements/velocities for the CDM particles in our simulations, which are generated using GRAFIC (Bertschinger 1995), again using $\Omega_{\text{CDM}} = 0.28$, $\Omega_{\Lambda} = 0.72$, and $\sigma_8 = 0.88$. An example of the final density field at redshift $z = 0$ is shown in Figure 1 for comparison with the Λ CDM simulation.

We look for all virialized isolated halos within our computational volume using a spherical overdensity algorithm. For this purpose, we employ a time-varying virial density contrast which is determined using the fitting formula presented in Mainini et al. (2003), and adopt the same virial density contrast for all models. In addition, we include all haloes with more than 200 particles into the halo catalog (see Macciò et al. 2008 for further details on our halo finding algorithm). Power spectra have been computed through a (fast) Fourier transform of the matter density field, computed on a regular grid $N_G \times N_G \times N_G$ from the particle distribution via a cloud-in-cell algorithm (see Casarini et al. 2009). We set $N_G = 256$ which gives a maximum mode of $k \approx 20 h \text{ Mpc}^{-1}$ well above the simulation resolution.

In Figure 2, we show the mass functions for the runs with $\gamma = 1.0, 0.5$, and $\mu = 10^{-5}, 10^{-6}, 10^{-7}$ and the fiducial Λ CDM simulation at two output redshifts $z = 1$ and 0 . The nonlinear matter power spectra of these models are displayed in Figures 3 and 4, respectively.

3.3. Interpretation of the Results

The results of the N -body simulations can be understood intuitively, as we shall discuss below. In general, a scalar field coupled to matter particles produces a fifth force (cf. Equation (11)) on the latter, which has a finite range m_{ϕ}^{-1} determined by the mass m_{ϕ} of the scalar field. If m_{ϕ} is small and almost constant across space then the fifth-force effect

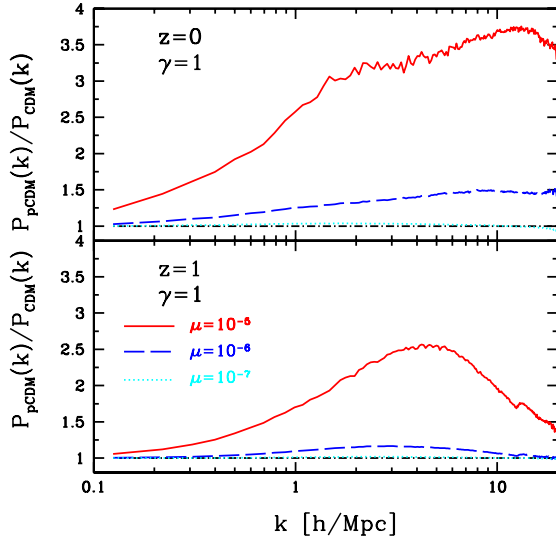


Figure 3. Ratios of calculated nonlinear matter power spectra for $\gamma = 1$ and $\mu = 10^{-5}$ (solid), 10^{-6} (dashed), and 10^{-7} (dotted) as well as for that of Λ CDM. Shown are results for two redshifts, $z = 1, 0$. At large scales (small k), the curves converge to the horizontal curves (identical to 1, dot-dashed). Note that, using analytic results, the difference is expected to be small on both large and very small scales, and decreases at higher redshift. Error bars of future lensing observations are likely small enough to detect any deviation from Λ CDM on intermediate scales ($k = 0.1\text{--}10 h \text{ Mpc}^{-1}$) at a 30% level.

(A color version of this figure is available in the online journal.)

essentially leads to an increase in the effective gravitational constant which governs structure formation (Macciò et al. 2004). Li & Zhao (2009) have shown that for certain regions of parameter space and specific choices of the potential, this is indeed a good approximation. Mathematically, this corresponds to neglecting the source terms starting with Λ_0 in Equations (8) and (9); hence the fifth force $\gamma \nabla \phi$ is about a factor $2\gamma^2$ times the gravitational force $\nabla \Phi/a$.

In another situation, when the scalar field has a very steep potential, m_ϕ depends sensitively on the local matter density (Khouri & Weltman 2004) so that it almost resides at the minimum of its effective potential,

$$V_{\text{eff}}(\phi) = V(\phi) + 8\pi G \rho_{\text{CDM}} \exp(\gamma\phi), \quad (12)$$

throughout space, i.e., $\phi \sim \Lambda_0 \mu / (8\pi G \rho_{\text{CDM}})$. This is known as the chameleon effect whose direct consequence is that in a high-density environment, m_ϕ^2 gets very heavy,

$$m_\phi^2 = \partial^2 V_{\text{eff}} / \partial \phi^2 = \Lambda_0 \mu (1 + \mu) \phi^{-\mu-2} \propto \mu^{-1} \rho_{\text{CDM}}^{-2}, \quad (13)$$

and the fifth force becomes very short-ranged, with its effect being suppressed due to $\gamma \nabla \phi \propto \gamma \mu \nabla \rho_{\text{CDM}}^{-1}$. In general, the smaller μ is, and/or the larger $\gamma, \rho_{\text{CDM}}$ are, the heavier m_ϕ becomes and thus the stronger the chameleon effect will be. Furthermore, since the value of ϕ inside a region also depends on its boundary condition, which in our case matches the background $\bar{\phi}$ asymptotically, we see that a smaller $\bar{\phi}$ leads to a smaller ϕ and a heavier m_ϕ , and therefore to a stronger chameleon effect.

There are several interesting features in Figure 2 which can be understood schematically. First of all, our models produce more halos within the considered mass range than Λ CDM due to the enhancing effect of the fifth force. Second, a smaller μ means that the fifth force is more severely suppressed by the chameleon effect, and thus causes a small deviation from

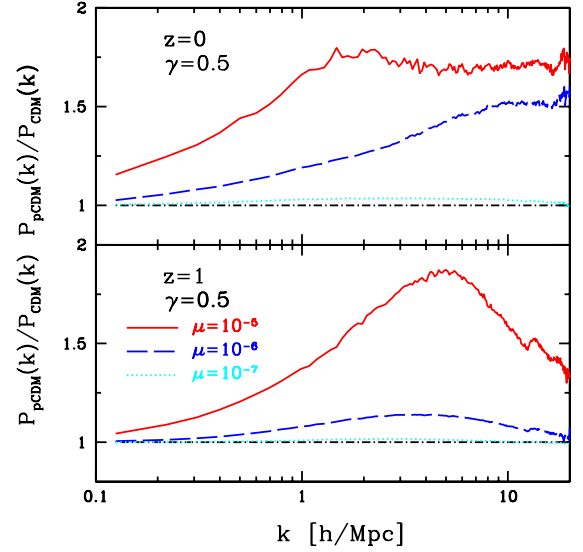


Figure 4. Same as Figure 3, but for $\gamma = 0.5$.

(A color version of this figure is available in the online journal.)

Λ CDM. Thirdly, a larger ρ_{CDM} also means that the fifth force is more severely suppressed, and this is why at high redshifts the deviation from Λ CDM (for the same γ and μ) is smaller. Fourthly, the influence of the parameter γ is more complicated: a larger γ will strengthen the chameleon effect, tending to suppress the fifth force, but at the same time it increases the magnitude of the fifth force. In cases where the chameleon effect is weak (e.g., $\mu = 10^{-5}$), however, we do see that a larger γ leads to larger deviations from Λ CDM.

Also note that the deviation from the Λ CDM mass function is more significant toward the low-mass end. To understand why this is the case, consider a mass range $[M_0, M_0 + \Delta M]$. At a certain redshift, some halos which should have been in this range in Λ CDM indeed fall into the mass range $(M_0 + \Delta M, \infty)$ in our model as the fifth force accelerates the formation of structures (this tends to reduce the number of halos with mass $> M_0$ as two halos which are separated in Λ CDM merge into one here), while some halos which should have been in the mass range $< M_0$ in Λ CDM actually fall in the mass range $[M_0, M_0 + \Delta M]$ in our model (this increases the number of halos with mass $> M_0$). This effect is weaker for the largest halos because of competing effects due to merging of small halos. As the mass increases, the difference between the mass functions of the two models narrows down.

In the matter power spectrum, we see something similar: smaller μ and larger ρ_{CDM} (higher redshift) severely suppress the fifth force and lead to smaller deviations from Λ CDM; increasing γ strengthens the fifth force, thereby causing large deviations from Λ CDM. Interestingly, the deviation becomes largest on intermediate scales: large scales are beyond the probe of the fifth force, and thus not significantly affected, while the density on small scales is high and the fifth force is suppressed.

4. CONCLUSION

We have presented a general framework to study nonlinear structure formation in coupled scalar field models, in particular the models of Li & Zhao (2009). While these models are virtually indistinguishable from Λ CDM on both very large and very small scales, intermediate scales at low redshift ($z \lesssim 1$) relevant for galaxy clusters ($\sim 10^2\text{--}10^3 \text{ kpc}$) open a new window to test and constrain the interesting part of the parameter space.

On these scales, the matter power spectrum is significantly increased compared to that of Λ CDM. Observationally, this would most likely appear as a change of σ_8 on the order of 15%–20% for models with $\gamma = 0.5$ –1 and $\mu = 10^{-6}$ (see Figure 2). Any variation of σ_8 seems to be lower than 30% for current lensing measurements such as the Canada–France–Hawaii Telescope Legacy Survey (e.g., Hoekstra et al. 2006; Figure 11 of Fu et al. 2008) over a rather limited range; however, future surveys, such as the Kilo-Degree Survey, will be able to measure the scale dependence within the range $k = 0.1$ – $10 h \text{ Mpc}^{-1}$, where the deviation of the models from Λ CDM is maximal.

This work has been performed within the HPC-EUROPA project, with the support of the European Community Research Infrastructure Action under the FP8 “Structuring the European Research Area” Programme. We thank Simon-Porteges Zwart and Marco Baldi for discussions. H. Zhao is thankful for financial support from the Dutch NWO visitorship No.040.11.089 to Henk Hoekstra, B. Li acknowledges financial support from a UK Overseas Research Studentship, the Cambridge Overseas Trust and Queens’ College Cambridge. M. Feix is supported by a scholarship from the Scottish Universities Physics Alliance (SUPA).

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